A Prior-Free Encode-Decode Change Detection Test to Inspect Datastreams for Concept Drift

Cesare Alippi¹², Li Bu¹, Dongbin Zhao¹

- 1. State Key Laboratory of Management and Control for Complex Systems, Institute of Automation Chinese Academy of Sciences
- 2. Dipartimento di Elettronica e Informazione, Politecnico, di Milano, 20133 Milano, Italy

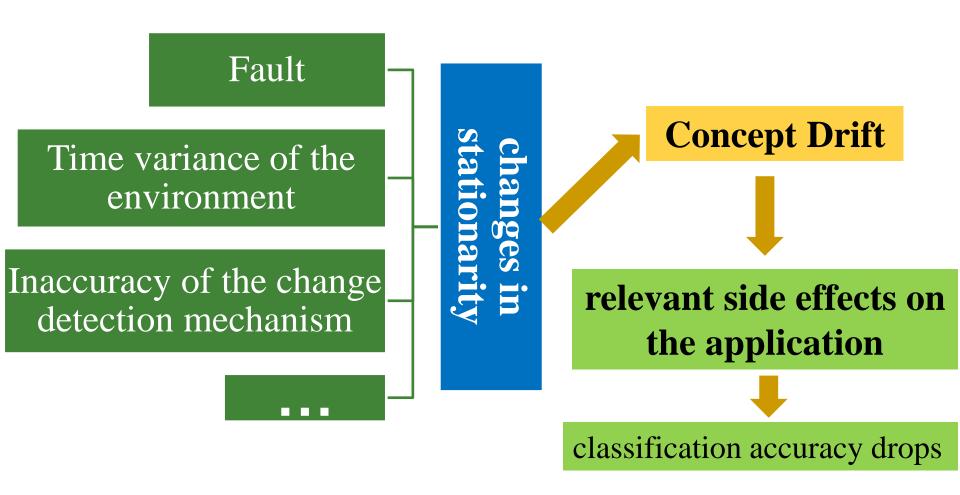
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- The Quest for Change Detection
- Encode-Decode Machine
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- Experimental Validation
- Conclusions



The Quest for Change Detection

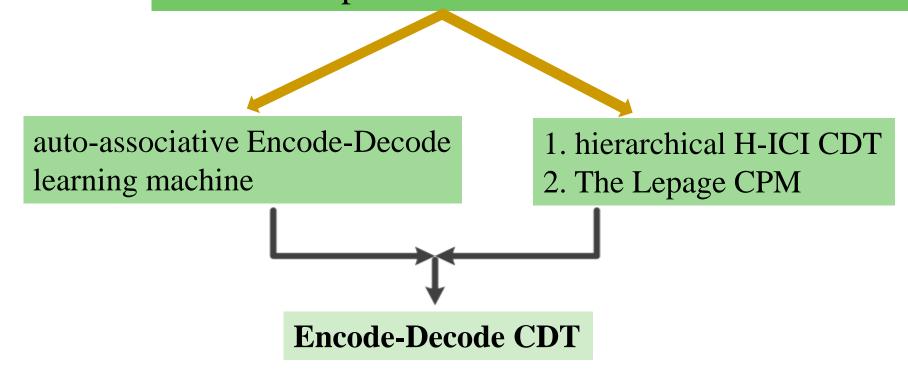




The Quest for Change Detection

The aim

to develop a novel and effective change detection test which operates in the residual framework





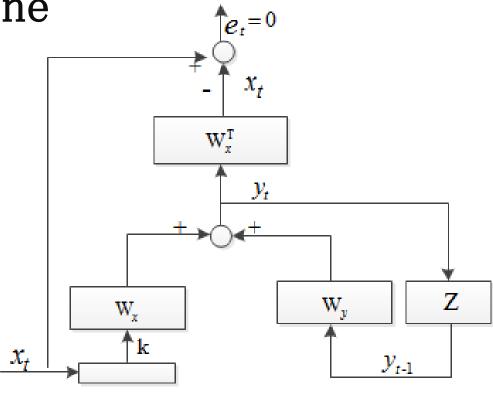
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$$y_t = W_x x_t + W_y y_{t-1}$$

satisfy the constraints:

$$x_t = W_x^T y_t$$
$$y_{t-1} = W_y^T y_t$$



Sufficient conditions to design the machine in [1] require:

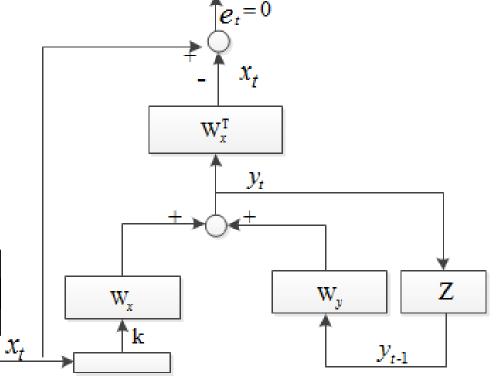
- 1. the columns of W_x to be orthogonal to those of W_y
- 2. $W_x^T W_x$ and $W_y^T W_y$ must be projector matrices applied to vectors X_t and Y_t



 y_t , W_y and W_x are defined as:

$$\mathbf{y}_{t}^{T} = \left[\mathbf{x}_{t}^{T}, \mathbf{x}_{t-1}^{T}, \dots, \underbrace{\mathbf{0}^{T}, \dots, \mathbf{0}^{T}}_{q-t+1} \right]$$

$$W_{y} = \begin{bmatrix} 0_{k,kq} & 0_{k,k} \\ I_{kq,kq} & 0_{kq,k} \end{bmatrix}; W_{x} = \begin{bmatrix} I_{k,k} \\ 0_{kq,k} \end{bmatrix}_{x_{t}}$$



k is the length of vector x_t , q is the memory depth of this machine, and define s = k(q+1).



To reduce the complexity, Construct at first matrix $X_{\tau,s}$ for each row vector y_t , $t = 1,...,\tau$ and compute the SVD

$$X_{\tau,s} = U_{\tau,\tau} \sum_{\tau,s} V_{s,s}^T$$

Keep the first p singular values and the associated eigenvetors to compose \tilde{V} .

$$\tilde{V}^T \tilde{V} = I_{p,p}$$

Define $y_t = V^T y_t$, and $V^T W_y y_{t-1} = V^T W_y V V^T y_{t-1}$ when $p \, ^3 rank(S_{t,s})$

$$\widetilde{y}_{t} = \widetilde{V}^{T} W_{x} x_{t} + \widetilde{V}^{T} W_{y} \widetilde{V} y_{t-1}$$



$$\widetilde{y}_{t} = \widetilde{V}^{T} W_{x} x_{t} + \widetilde{V}^{T} W_{y} \widetilde{V} y_{t-1}$$

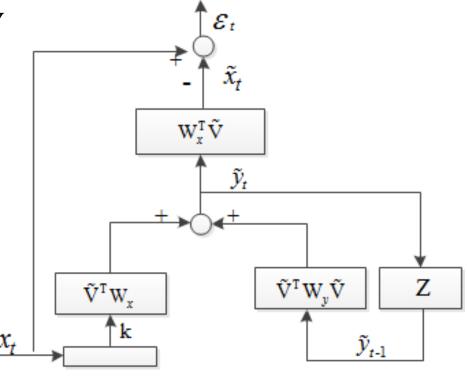
represents an approximate expression when $p < rank(S_{t,s})$

Define
$$W_x = V^T W_x$$
, $W_y = V^T W_y V$

$$y_t = W_x x_t + W_y y_{t-1}$$

$$\tilde{x}_t = W_x^T y_t$$

$$\varepsilon_t = x_t - \tilde{x}_t = W_x^T (I_{s,s} - \tilde{V}\tilde{V}^T) y_t$$





Select the *p* maximizing the whiteness of the reconstruction residual

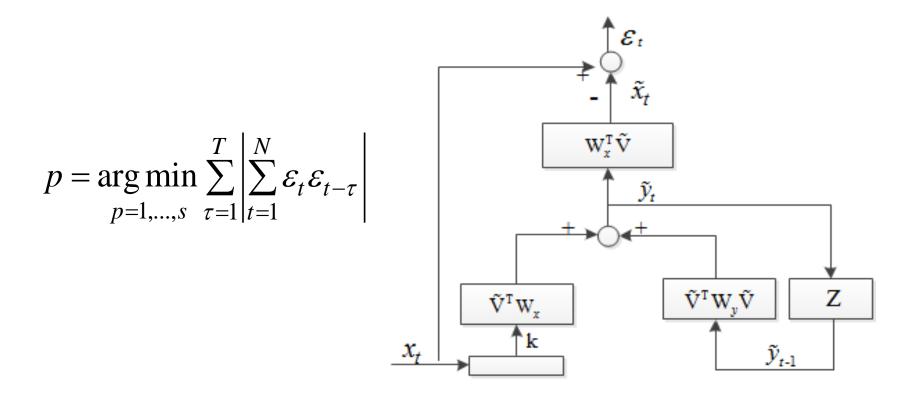


Fig.1 the Encode-Decode SVD-reduced machine



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A. Detecting Changes with the Designed Encode-Decode Machine

$$\varepsilon_t = W_x^T (I_{s,s} - \tilde{V}\tilde{V}^T) y_t = (I_{s,s} - \tilde{V}\tilde{V}^T)_{k,s} y_t$$

the first component of the error vector \mathcal{E}_t

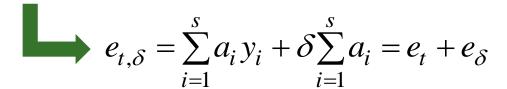
$$e_t = \sum_{i=1}^{s} a_i y_i = a^T y_t$$

 a_i is the *i*-th entry of the first row a of the matrix $(I_{s,s} - VV^T)$



(1). Abrupt Perturbation Case

$$x_{\delta}(t) = x(t) + \delta$$
, $t > t_p$ $\delta(t) = \delta$ is an abrupt perturbation



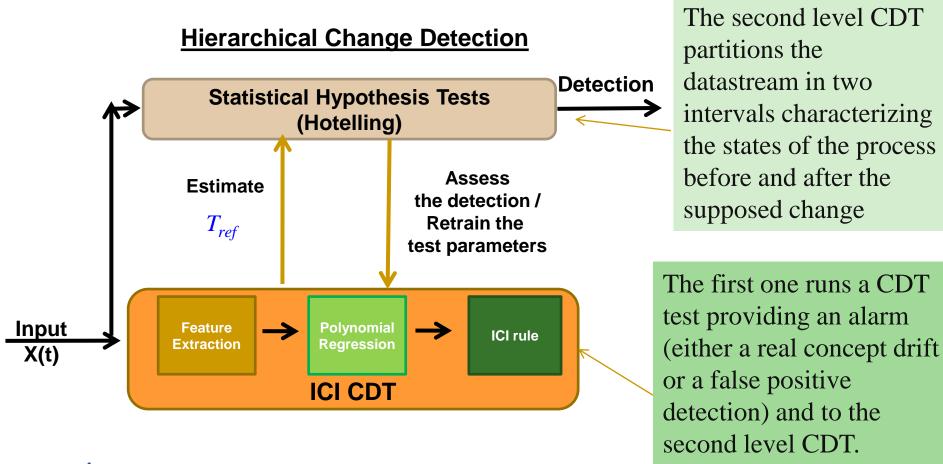
(2). Linear Drift Perturbation Case

$$x_{\delta}(t) = x(t) + \delta_d t$$
, $t > t_p$ $\delta(t) = \delta_d t$ is the perturbation drift.

$$e_{t,\delta} = \sum_{i=1}^{s} a_i y_i + \delta \sum_{i=1}^{s} a_i t = e_t + e_{\delta}$$

B. H-ICI CDT and Lepage CPM

(1). H-ICI CDT



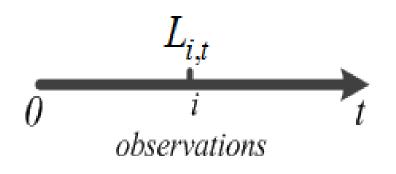


(2). Lepage CPM

The rank of the *i*-th observation at time *t* is defined as

$$r(x_i) = \sum_{i \neq j}^{t} I(x_i > x_j)$$
 I is the indicator function

Combine the Mann-Whitney test statistic U and the Mood test statistic M. $L = U^2 + M^2$ is used.



$$\overline{L} = \max_{0 < i \le t} L_{i,t}$$

a change is detected when $\overline{L}^{\, 3} h_t$ (h_t is a given threshold)



C. Designing the Encode-Decode CDT

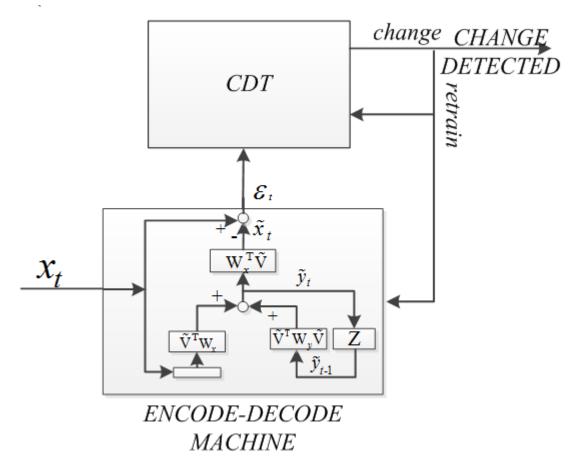


Fig.2 Encode-Decode machine



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The reference application comes from the data acquired from the hybrid wired-wireless monitoring system deployed on the Alps to monitor a potential rock collapse.

Data, here temperature, are sampled every 5 minutes and sent to a remote control station for subsequent processing.

Training set: 3000 samples k = 1, q = 3

Validation set: 1000 samples p = 2

Testing set: change is injected randomly around sample 1000

Parameters of CDT: gamma.H-ICI=0.5; ARL0.CPM=40000



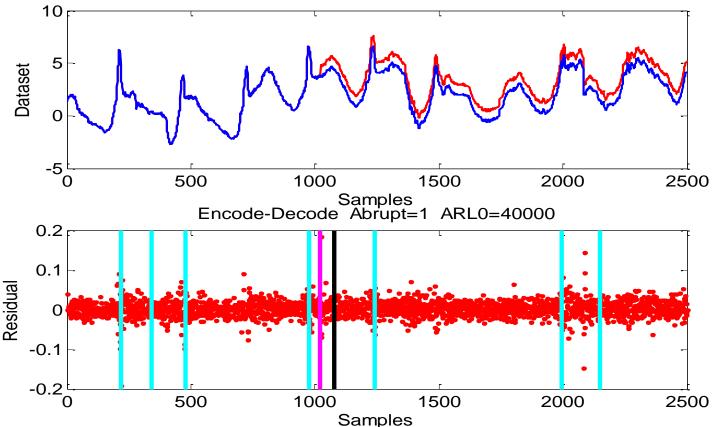


Fig. 3. An abrupt change occurring around point 1000 affects the sensor measurements. (In the upper plot, the blue line represents the initial data, and the red line shows the data with the added change. In the lower plot, the pink vertical line represents the time of the change occurrence, the black one represents the detection of the H-ICI CDT and the cyan one that of the CPM-LP test)



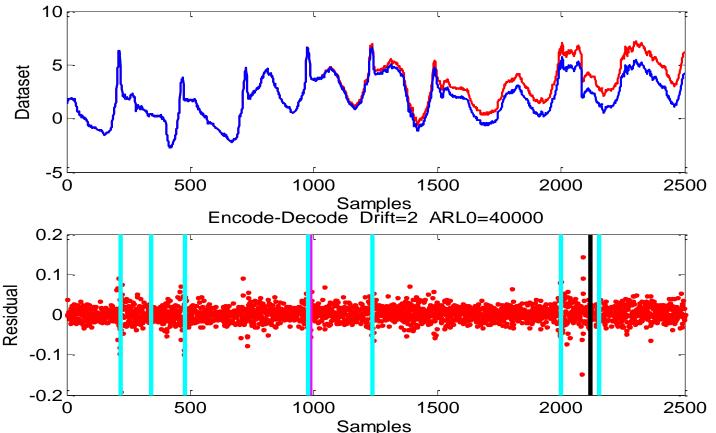


Fig. 4. A linear drift affects the sensor measurements. (In the upper plot, the blue line represents the initial data, and the red line shows the data with the added change. In the lower plot, the pink vertical line represents the start time of change occurrence, the black one is the detection of the H-ICI CDT and the cyan line that of the CPM-LP)



TABLE I The Performance Comparison Of The Encode-Decode Machine And AR With H-ICI And CPM-LP CDT

Change	d	Encode-Decode machine + H-ICI			AR + H-ICI			Encode-Decode machine + CPM-LP			AR + CPM-LP		
		FP	FN	L	FP	FN	L	FP	FN	L	FP	FN	L
Abrupt	0.1	0%	100%	- (-)	0%	100%	- (-)	100%	0%	214.8 (65.4)	100%	0%	208.3 (57)
	0.4	0%	59%	76.7 (50.7)	0%	100%	- (-)	100%	0%	213.3 (67)	100%	0%	621 (404.8)
	0.5	0%	25%	85.2 (54.5)	0%	100%	- (-)	100%	0%	201.9 (77.1)	100%	0%	648.4 (404.8)
	1	0%	6%	84.3 (35.8)	0%	7%	1077.1 (161.7)	100%	0%	199.7 (85.3)	100%	0%	875.3 (307.8)
Drift	0.5	0%	100%	- (-)	0%	100%	- (-)	100%	0%	190.5 (84.8)	100%	0%	207.2 (54)
	1	0%	100%	- (-)	0%	100%	- (-)	100%	0%	200.3 (79.9)	100%	0%	199.1 (68.4)
	1.5	0%	0%	1341.5 (20.1)	0%	100%	- (-)	100%	0%	197 (83.7)	100%	0%	208.6 (57.5)
	2	0%	0%	1119.7 (17.5)	0%	100%	- (-)	100%	0%	208.2 (72)	100%	0%	209.4 (54.1)
	20	0%	0%	218.4 (115.7)	0%	0%	1057.4 (23.2)	100%	0%	190.4 (84.8)	100%	0%	207.1 (54)
	18		/				8						

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Conclusions

- The paper presents a new mechanism for generating a residual sequence to be inspected for potential concept drift.
- The method is based on an auto-associative recurrent machine whose computational complexity is controlled with a SVD decomposition.
- The outcome is a novel change detection test we name Encode-Decode CDT.
- The method, applied to a real application shows the effectiveness.



Thanks!

