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# Applications of Homomorphic Functions to Software Obfuscation\*

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## 1 Introduction

As various computers are connected into a world wide network, software is a target of copyright pirates, attackers, or even terrorists, as a result, software protections become a more and more important issue for software users and developers. There are some technical measures for software protections, such as hardware-based protections and software-based techniques [1], etc. Software obfuscation [2] is one of these measures to protect software from unauthorized modification by making software more obscure so that it is hard for potential attackers to understand the obfuscated software. There are several algorithms of software obfuscation such as layout transformation, computation transformation, ordering transformation, and data transformation [2]. Variable transformation is a major method of data transformation to transform software into a new semantically equivalent one that is hard for attackers to understand the true meaning of variables in software.

Chow et al. applied residue number technique, an approach used in hardware design, high precision integer arithmetic, and cryptography, to software obfuscation by encoding variables in the original program to hide the true meaning of these variables [3], but part of the technique proposed there is incorrect. In order to compensate this drawback, in paper [4], we proposed homomorphic functions, developed an algorithm for division by several constants based on homomorphic functions, and applied them to variable transformation.

Data structures are important components of programme and they are key clues for people to understand codes. Obfuscating data structures of programme will make it very hard for an attacker to modify them. In this paper, we apply homomorphic functions to obfuscate arrays in software through array index change, array index and dimension change, array folding, and array flattening. As said in [2], by adding the data complexity in the program, these methods can make a program much more difficult to understand and reverse engineer. We are investigating the security of these applications.

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## 2 Application of Homomorphic Functions to Array's Change

We describe four methods to apply homomorphic functions to software obfuscation: index change, index and dimension change, array folding and array flattening.

### 1. Index change

For an array  $A[n]$ , firstly, find an  $m$  such that  $m > n$ , and  $n$  and  $m$  are relatively prime, then change  $A[n]$  into  $B[n]$  and the element  $A[i]$  is turned into  $b[i * m \bmod n]$ .

### 2. Index and dimension change

For an array  $A[n]$ , firstly, find an  $m$  such that  $m > n$ , and  $n$  and  $m$  are relatively prime, then change  $A[n]$  into array  $B[m]$  and the element  $A[i]$  is turned into  $b[i * n \bmod m]$ .

### 3. Array folding

For an array  $A[n]$ , we assume  $n > 2$ . The array folding procedure is as follows.

If  $n$  is a prime, let  $m = n + 1$ ; otherwise  $m = n$ .

Extend  $A[n]$  into  $C[m]$  by  $C[i] = A[i]$  for  $0 \leq i < n$  and  $C[i]$  undefined for others.

Factor  $m$  into  $m_1$  and  $m_2$ . Replace  $C[m]$  with  $B[m_1, m_2]$  through  $B[i \bmod m_1, i \bmod m_2] = C[i]$  for  $0 \leq i < m$ .

Replace any  $A[i]$  with  $B[i \bmod m_1, i \bmod m_2]$  in the unobfuscated program.

### 4. Array flattening

For a 2-dimensional array  $A[n_1, n_2]$ , the array flattening procedure is as follows.

Find two relatively prime integers  $m_1$  and  $m_2$  such that  $n_1 \leq m_2$  and  $n_2 \leq m_2$ . Let  $m = m_1 * m_2$ .

Turn the 2-dimension array  $A[n_1, n_2]$  into another 2-dimension array  $C[m_1, m_2]$  by  $C[i, j] = A[i, j]$  for  $0 \leq i < m_1$  and  $0 \leq j < m_2$ , and  $C[i, j]$  undefined otherwise. Replace all  $A[i, j]$  with  $C[i, j]$ .

Find two relatively integers  $k_1$  and  $k_2$  such that  $k_1 * m_1 + k_2 * m_2 = 1$ .

Turn the 2-dimension array  $C[n_1, n_2]$  into a 1-dimension array  $B[m]$  and let  $B[i] = C[i \bmod m_1, i \bmod m_2]$  for  $0 \leq i < m$ .

Replace any  $A[i, j]$  with  $B[(i * k_1 + j * k_2) \bmod m]$  for  $0 \leq i < n_1$  and  $0 \leq j < n_2$ .

## 3 Conclusion

We propose applications of homomorphic functions to obfuscate arrays in software.

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